Computational interferometric imaging

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imaging.cs.cmu.edu/interferometry_siggraph2023

Today's presenters



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What is interferometry?

OCT eye exam OD(R) Overlay Grid optical coherence tomography angiographer Overlay Grid Layers 128retinal tomographic scan

Retinal scanning and angiography to diagnose glaucoma, diabetic retinopathy, macular degeneration, etc.

"Around 64% of adults working in computer and mathematical sciences use some vision correction option" (i.e., glasses, contacts, surgery) From the Washington Post, May 2023

[Images from the American Academy of Ophthalmology]

Skin cancer imaging



Non-invasive imaging of breast and dorsal skin tumors

(Still at the pre-clinical level)



2 mm depth 10 µm resolution

[Images from Vakoc et al. 2012, Nature Reviews Cancer]

Seeing deep inside tissue

NSF Expedition project, https://seebelowtheskin.org

The need for micrometer resolutions

50 µm

[Image from Wikimedia Commons]

FMCW "4D" lidar



Depth *and* velocity using frequency-modulated continuous-wave lidar (a.k.a. swept-source optical coherence tomography)

[Images from Aeva, and Zhang et al. 2019]

[Images from Kotwal et al., 2023]

Micrometer 3D sensing

Inspection: aircraft fuselage section



Fabrication: 3D-printed Euro coin



Very large-scale physics



first gravitational wave detection



Laser Interferometer Gravitational-wave Observatory (LIGO) at Hanford, WA (4 km-long Michelson interferometer)



first image of a black hole (center of Messier 87 galaxy)



Location of observatories making up the Event Horizon Telescope (EHT) (very-long-baseline interferometry)

Computational imaging



Non-line-of-sight imaging



Transient imaging



Separation of direct-indirect illumination

Course overview



Course overview



Interferometric imaging



Interferometric imaging



Interferometer designs





Interferometer implementations





Phase-shifting interferometry





Phase-shifting interferometry

Interference: correlation of two reference mirror sinusoids \rightarrow another sinusoid of sample frequency and phase $\delta \varphi$ $\delta \varphi$ singletilted d_{t} frequency mirror laser



Example: surface deflectometry with PSI



Example: surface deflectometry with PSI



Phase-shifting interferometry:

sub-wavelength resolution

- × wavelength depth range
- × only for smooth surfaces
- × very sensitive to vibrations

x very sensitive to aberrations

Course overview



Computational 3D Imaging and Measurement (3DIM) Lab

Current Members

THE UNIVERSITY OF ARIZONA Wyant College of Optical Sciences

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Florian Willomitzer - Computational 3D Imaging and Measurement Lab - www.optics.arizona.edu/3dim

Part 2:

Interferometry on Rough Surfaces and Synthetic Wavelengths

Florian Willomitzer

Associate Professor Wyant College of Optical Sciences University of Arizona, USA

https://www.optics.arizona.edu/3dim



Computational **3D** Imaging and Measurement Lab

Prof. Florian Willomitzer



THE UNIVERSITY OF ARIZONA Wyant College of Optical Sciences



A

Coherent imaging on rough surfaces - Speckle





Coherent imaging on rough surfaces - Speckle



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When is a surface "optically rough"?





When is a surface "optically rough"?





Approaches measuring the Time-of-Flight of ligth





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<u>Millimeter-sized waves with visible light?</u>

NO! ... well ... let's look at sound waves!





Synthetic Waves



Fercher et al., Applied Optics 24(14) (1985) Dändliker et al., Optics Letters 13(5) (1988)



High-precision "ToF Camera"





$E(\Lambda) = E(\lambda_1) \cdot E^*(\lambda_2)$ = $A_1 A_2 \cdot \exp(i(\phi(\lambda_1) - \phi(\lambda_2)))$

F. Li*, F. Willomitzer*, M. Balaji, P. Rangarajan, O. Cossairt, Exploiting Wavelength Diversity for High Resolution Time-of-Flight 3D Imaging, IEEE Transactions on Pattern Analysis and Machine Intelligence (TPAMI), 2021





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High-precision "ToF Camera"



Sub-mm depth resolution easily achievable!

F. Li^{*}, F. Willomitzer^{*}, M. Balaji, P. Rangarajan, O. Cossairt, Exploiting Wavelength Diversity for High Resolution Time-of-Flight 3D Imaging, IEEE Transactions on Pattern Analysis and Machine Intelligence (TPAMI), 2021



EXPERIMENT 11

<u>Sidenote</u>

Synthetic wavelengths are also useful in absence of scattering!



Optical phase \rightarrow strong wrapping! $\lambda = 854.3 nm$





Y. Wu*, F. Li*, F. Willomitzer, A. Veeraraghavan, O. Cossairt, WISHED: Wavefront Imaging Sensor with High resolution and Depth ranging, EEE International Conference on Computational Photography (ICCP), 2020



EXPERIMENT

0
How to detect the synthetic field $E(\Lambda)$?

(or the two optical fields $E(\lambda_1), E(\lambda_2)$)

- Phase shifting
- Temporal heterodyning
- Spatial heterodyning
- Iterative phase retrieval
- Deep learning

→ Vast playfield!

→ No free lunch!

Better question to ask by an "adopter":

What are important modalities for your application?

- Full field
 - Single-shot
 - Reference-less
 - No prior object knowledge
- COTS CCD/CMOS cameras





1

0.8

0.6

0.4

0.2

0

 2π

π

Susceptibility to motion



M. Ballester*, H. Wang*, J. Li, O. Cossairt, F. Willomitzer. 'Single-shot ToF sensing with sub-mm precision using conventional CMOS sensors', Arxiv Preprint, 2022



Solution: Single-shot acquisition



'Single-shot ToF sensing with sub-mm precision using conventional CMOS sensors', Arxiv Preprint, 2022



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Reminder last slide:



Solution: Single-shot acquisition



Takeda et al., JoSA 72(1), 1982

M. Ballester*, H. Wang*, J. Li, O. Cossairt, F. Willomitzer. 'Single-shot ToF sensing with sub-mm precision using conventional CMOS sensors', Arxiv Preprint, 2022



ENT 17

<u>**Results**</u> (single-shot)

Object



Small figure

 $\phi_{wrapped}(\Lambda=10mm)$



 $\phi_{unwrapped}(\Lambda = 10mm)$



3D model $\Lambda = 10mm$ $\delta z \approx 1.8mm$



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Quantitative analysis of distance precision δz

Λ [mm]	40	10	5	3	1
$\delta z_{\text{single}} \text{ [mm]}$	5.56	1.78	1.64	0.79	0.33



 $\Lambda = 50mm$



 $\Lambda = 10mm$

M. Ballester*, H. Wang*, J. Li, O. Cossairt, F. Willomitzer. 'Single-shot ToF sensing with sub-mm precision using conventional CMOS sensors', Arxiv Preprint, 2022



<u>Results</u> (dual shot)

Object



Clay pot

 $\phi_{wrapped}(\Lambda = 3mm)$



 $\phi_{unwrapped}(\Lambda = 3mm)$



3D model $\Lambda = 3mm$ $\delta z \approx 0.8mm$



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ᡵ Florian Willomitzer - Computational 3D Imaging and Measurement Lab - www.optics.arizona.edu/3dim



Object



Small figure

Jal-shot vs.

3D model $\Lambda = 10mm$



Single-shot





Video acquisition

Object:

metronome 10 mm

3D Video



M. Ballester*, H. Wang*, J. Li, O. Cossairt, F. Willomitzer. 'Single-shot ToF sensing with sub-mm precision using conventional CMOS sensors', Arxiv Preprint, 2022



End Part 2



Course overview



Fiber-based interferometry



reference arm

Time-domain optical coherence tomography



reference arm

Time-domain optical coherence tomography



Time-domain optical coherence tomography



Frequency-domain optical coherence tomography



Swept-source optical coherence tomography



Swept-source optical coherence tomography



Full-field OCT





Micron-scale shape scanning

depth resolution ~5 μm



 full-field OC⊤	full-field SWI

	full-field OCT	full-field SWI
depth range	constrained by reference translation	synthetic wavelength (separation between wavelengths)
phase wrapping	no	yes

	full-field OCT	full-field SWI
depth range	constrained by reference translation	synthetic wavelength (separation between wavelengths)
phase wrapping	no	yes
depth resolution	spectral bandwidth	separation between wavelengths

	full-field OCT	full-field SWI	
depth range	constrained by reference translation	synthetic wavelength (separation between wavelengths)	
phase wrapping	no	yes	
depth resolution	spectral bandwidth	separation between wavelengths	
scanning	axial proportional to depth range OR lateral proportional to scene size	fixed axial scanning possibly single shot!	

	full-field OCT	full-field SWI
depth range	constrained by reference translation	synthetic wavelength (separation between wavelengths)
phase wrapping	no	yes
depth resolution	spectral bandwidth	separation between wavelengths
scanning	axial proportional to depth range OR lateral proportional to scene size	fixed axial scanning possibly single shot!
measurement	full tomography	surface-only

Fiber v/s full-field



Cup: image formation

'direct'

╉

'retroreflective specular'





scene-only image

cup

Depth corruption due to indirect light



depth corruption

Image formation and light transport



light transport matrix

Image formation and light transport



light transport matrix

adding

Probing



Interferometric probing



Direct-indirect separation



Seeing through scattering



source




Dichromatic area light?





Swept-angle synthetic wavelength interferometry

Swept-angle SWI results: 1 mm depth range



no swept-angle scanning

ours, swept-angle

scene input image

Swept-angle SWI results: 1 mm depth range



Swept-angle SWI results: \$20 bill eagle



dollar bill

scene

recovered depth surface recovered depth map

Swept-angle SWI results: 1 cm depth range



no swept-angle scanning

ours, swept-angle

scene input image



Applications: industrial inspection



photo of scanned object

image of scanned scene

ours, swept-angle

without swept-angle



Applications: precision fabrication



photo of scanned object

image of scanned scene

ours, swept-angle

without swept-angle

Sudershan Boovaraghavan / Yuvraj Agrawal



Course overview



Part 4:

Non-Line-of-Sight imaging ^{using} Synthetic Wavelengths

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Computational **3D** Imaging and Measurement Lab

Prof. Florian Willomitzer



THE UNIVERSITY OF ARIZONA Wyant College of Optical Sciences



Wyant College of Optical Sciences

Imaging around Corners



Imag. through Scattering Media



F. Willomitzer et al., Nature Communications 12, 6647 (2021)







$$E(\Lambda) = E(\lambda_1) \cdot E^*(\lambda_2)$$

= $A_1 A_2 \cdot \exp(i(\phi(\lambda_1) - \phi(\lambda_2)))$

F. Li*, F. Willomitzer*, M. Balaji, P. Rangarajan, O. Cossairt, Exploiting Wavelength Diversity for High Resolution Time-of-Flight 3D Imaging, IEEE Transactions on Pattern Analysis and Machine Intelligence (TPAMI), 2021



SIMULATION 27

Willomitzer et al., Nature Synthetic Wavelength Holography Communications 12, 6647, 2021 **CW** Tunable Object Laser Source Detector Λ $|E(\lambda_2)|$ $|E(\lambda_1)|$ $\phi(\lambda_1)$ $\phi(\lambda_2)$ Scatterer (Tissue, Ψ_{max} Rough Wall, Fog, ...) Λ $|E(\Lambda)|$ $E(\lambda_1) \cdot E^*(\lambda_2)$ $= \boldsymbol{E}(\boldsymbol{\Lambda})$ Numerical Backpropagation at Λ Computational Hologram **Synthesis** Reconstruction

Reconstruct

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Experiment: Looking around corners





Imaging around corners at multiple SWLs



Fundamental limit

EXPERIMENT

Where is the limit?

Fundamental limit:

Tunable!
$$\Lambda \ge 4 \Psi_{max}$$
*

How to estimate the performance of our system?

Space-Bandwidth Product (SBP):



* Related calculations given in:

F. Willomitzer, P. Rangarajan, F. Li, M. Balaji, M. Christensen, O. Cossairt, 'Synthetic Wavelength Holography: An Extension of Gabor's Holographic Principle to Imaging with Scattered Wavefronts', Arxiv 1912.11438 (2019)



Experiment: Imaging through Scattering Media



Willomitzer et al., 2021

Imaging through scatterers - Results





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Synthetic Pulse Holography/Interferometry

<u>Computational</u> coherent superposition of multiple synthetic holograms \rightarrow "synthetic pulse"



\rightarrow Similarity to OCT, WLI, light-in-flight imaging, transient imaging

F. Willomitzer, P. Rangarajan, F. Li, M. Balaji, M. Christensen, O. Cossairt, 'Fast Non-Line-of-Sight Imaging with High-Resolution and Wide Field of View using Synthetic Wavelength Holography', Nature Communications 12, 6647 (2021)

P. Cornwall, M.Ballester, H. Wang, F.Willomitzer, 'Towards Synthetic Light-in-Flight', Optica Comp. Optical Sensing and Imaging (2023)



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Transient imaging





transient imaging using interferometry at 1000x larger temporal resolution

Transient imaging



[Velten et al. 2013]



transient imaging using interferometry at 1000x larger temporal resolution





[Images from Gkioulekas et al., 2015]

Chess knight and mirror



[Images from Gkioulekas et al., 2015]

Subsurface scattering



[Gkioulekas et al., 2015] scattering

paths transmitted through ground glass diffuse-diffuse reflections

Dispersion



[Images from Gkioulekas et al., 2015]

surface-wall reflections

rainbow

resolution

10⁻¹⁵ s

Non-line-of-sight (NLOS) imaging





what a regular camera sees

Non-line-of-sight (NLOS) imaging





what a regular camera sees

Picosecond-scale setup



ultra-sensitive lidar capturing later returns (single-photon avalanche diode)



Non-line-of-sight (NLOS) imaging





- Room-scale scanning (2 m x 2m)
- Object-scale scanning (0.5 m x 0.5 m)

Can we do this at micron scales?

Femtosecond-scale setup



interferometric time-of-flight setup

Micron-scale NLOS imaging



ground truth (LOS scan)

NLOS reconstruction

[Images from Xin et al., 2019]

Micron-scale NLOS imaging



horizontal location

ground truth (LOS scan)

interferometric setup resolution: $10 \mu m$ (33 fs)
Deploying interferometric systems is hard



typical interferometry setup

sunlight interferometry

Passive interferometry with sunlight



Sunlight interferometry



sun



Where we ran our experiments

Passive 3D sensing: Raspberry Pi



Passive transient imaging: metallic coin



[Images from Kotwal et al., 2023]

Passive transient imaging: diffuse pill



scene

transient response

depth

[Images from Kotwal et al., 2023]

Passive transient imaging: scattering chocolate



scene

transient response

depth

[Images from Kotwal et al., 2023]

Passive NLOS imaging

direct imaging





image

occluded imaging



scene



image



scene

depth [Images from Kotwal et al., 2023]



descattered image



depth



descattered image

Course overview





A coherent world...



Speckle rendering



what real laser images look like

what standard Monte Carlo renderings look like

A Monte Carlo Framework for Rendering Speckle Statistics in Scattering Media

CHEN BAR, Department of Electrical Engineering, Technion, Israel MARINA ALTERMAN, Department of Electrical Engineering, Technion, Israel IOANNIS GKIOULEKAS, Robotics Institute, Carnegie Mellon University, USA ANAT LEVIN, Department of Electrical Engineering, Technion, Israel



Fig. 1. **Simulation of memory effect in scattering.** Coherent images of translucent materials typically involve highly-fluctuating speckle structure. Despite their semi-random structure, speckles have strong statistical properties. For example, the memory effect property states that, as one tilts the illumination direction (setup at left), the resulting speckles shift. This property is at the core of multiple computational imaging applications. The memory effect is valid over a limited angular range that depends on material properties. Due to the absence of analytical formulas, it is generally necessary to measure this angular range for materials of interest empirically in the lab. We present a Monte Carlo rendering approach for simulating physically-accurate speckle images, as well as their statistics, as a function of material parameters. The figure shows speckle images rendered by our algorithm for a few illumination directions, as well as their auto-correlation (black insets), demonstrating the speckle shift property. As the angle difference increases, the correlation decays, and the decay rate is different for different material parameters—in this case, materials with Henyey-Greenstein (HG) phase functions of different parameters *g*. For the isotropic scattering case, *g* = 0, the pattern similarity is lost at the third column, whereas for the forward scattering case, *g* = 0.9, correlation is preserved. We verify the accuracy of our algorithm against an exact, yet computationally heavy, wave solver, as well as against analytical formulas derived under limiting assumptions.

Other coherent effects



https://en.wikipedia.org/wiki/Thin-film_interference



https://en.wikipedia.org/wiki/CD-ROM

thin film interference

 $\approx 1 \, \mu m$

diffraction

Some work in this area

A Generic Framework for Physical Light Transport

SHLOMI STEINBERG, University of California, Santa Barbara, USA LING-QI YAN, University of California, Santa Barbara, USA



TOM CUYPERS, TOM HABER and PHILIPPE BEKAERT Hasselt University and SE BAEK OH and RAMESH RASKAR MIT

We present a novel method of simulating wave effects in graphics using raybased renderers with a new function: the Wave BSDF (Bidirectional Scattering Distribution Function). Reflections from neighboring surface patches represented by local BSDFs are mutually independent. However, in many surfaces with wavelength-scale microstructures, interference and diffraction requires a joint analysis of reflected wavefronts from neighboring patches. We demonstrate a simple method to compute the BSDF for the entire microstructure, which can be used independently for each patch. This allows us to use traditional ray-based rendering pipelines to synthesize wave effects. We exploit the Wigner Distribution Function (WDF) to create transmissive, reflective, and emissive BSDFs for various diffraction phenomena in a physically accurate way. In contrast to previous methods for computing interference, we circumvent the need to explicitly keep track of the phase of the wave by using BSDFs that include positive as well as negative coefficients. We describe and compare the theory in relation to well-understood concepts in rendering and demonstrate a straightforward implementation. In conjunction with standard raytracers, such as PBRT, we demonstrate wave effects for a range of scenarios such as multibounce diffraction materials, holograms, and reflection of high-frequency surfaces.

Categories and Subject Descriptors: I.3.5 [Computer Graphics]: Computational Geometry and Object Modeling—*Physically based modeling*

General Terms: Algorithms, Theory



Fig. 1. We generalize the rendering equation and the BSDF to simulate wave phenomena. The new Wave BSDF behaves like a local scattering function, creates interference globally, and allows easy integration into traditional ray-based methods.



We still can't render an interferometer (for general scenes)

But it would be awesome if we could! Physics-based rendering and its applications in computational photography and imaging

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CVPR 2023 tutorial, imaging.cs.cmu.edu/pbr_cvpr2023

Many thanks to our collaborators!

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Manuel Ballester

Marc Christensen

Muralidhar Balaji

raraghavan

Oliver Cossairt

Patrick

Cornwall



Todd

Zickler



Yicheng Wu

Many thanks to our sponsors!



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SEE BELOW THE SKIN

Questions?

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